Seventh Semester B.E. Degree Examination, Aug./Sept.2020 Finite Element Modeling and Analysis

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

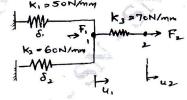
Module-1

a. Explain with neat sketch plane stress and plane strain.

(08 Marks)

b. For the spring system shown in Fig.Q.1(b) using principle of minimum potential energy determine the nodal displacement. Take $F_1 = 75N$ and $F_2 = 100N$. (08 Marks)

Fig.Q.1(b)



OR

2 a. Derive the equilibrium equation for 3D elastic body.

(08 Marks)

b. By RR method for a bar of cross section area A, elastic modulus E, subjected to uniaxial

loading P. Show that a distance X from fixed end is $u = \left(\frac{P}{AE}\right)X$

(08 Marks)

Module-2

a. What is FEA? Explain the basic steps involved in FEM.

(08 Marks)

b. Derive the stiffness matrix for the bar subjected to axial load F using direct method.

(08 Marks)

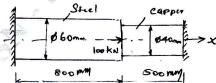
OR

- 4 a. What is shape function? Derive the shape function for 1D bar element in global coordinates.
 (08 Marks)
 - b. What are the convergence requirements? Discuss three condition of convergence requirement. (08 Marks)

Module-3

5 a. Determine the nodal displacement stress in each element and support reaction in the bar shown in Fig.Q5(a). (08 Marks)

Fig.Q5(a)



b. Solve the following system of simultaneous equation by gauss elimination method:

$$4x_1 + 2x_2 + 3x_3 = 4$$

$$2x_1 + 3x_2 - 5x_3 = 2$$

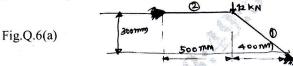
$$2x_1 + 7x_2 = 4$$

(08 Marks)

Important Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.

OR

6 a. For the two bar truss shown in Fig.Q.6(a). Determine the nodal displacements. Take $E = 2 \times 10^5 MPa$, $A = 200 mm^2$. (08 Marks)



b. Derive the elemental stiffness matrix for a truss element.

(08 Marks)

Module-4

- 7 a. Derive the shape function using lagrangian interpolation for linear Quadrilateral element.
 (08 Marks)
 - b. Briefly explain subparametric elements and super parametric elements.

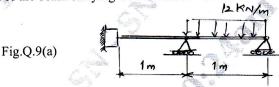
(08 Marks)

OR

- 8 a. Derive the hermite shape function for a 2 noded beam element. (08 Marks)
 - b. Briefly explain the finite element formulation of 2D Constant Strain Triangular Element (CST). (08 Marks)

Module-5

9 a. For the beam shown in Fig.Q.9(a). Determine the end reaction and deflection at the center of the portion of the beam carrying UDL. Take E = 200GPa $I = 4 \times 10^6$ mm⁴. (08 Marks)



b. Solve for temperature distribution in the composite wall as shown in Fig.Q.9(b) using 1D heat elements, use penalty approach of handling boundary conditions.

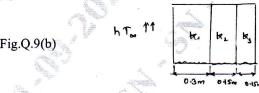
 $K_1 = 20 \text{W/m}^{\circ}\text{C}$

 $K_2 = 30 \text{W/m}^{\circ}\text{C}$

 $T_0 = 20^{\circ}C$

 $K_3 = 50 \text{W/m}^{\circ}\text{C}$

 $h = 25W/m^2C$



(08 Marks)

OR

- 10 a. Derive the expression for stiffness matrix for 1D heat conduction. (08 Marks)
 - b. For the beam element shown in Fig.Q.10(b). Determine deflection under the given load. Take $E = 2 \times 10^8 \text{kN/m}^2$ and $I = 4 \times 10^{-6} \text{m}^4$ (08 Marks)

